TRACE OF GENERATING SAMPLE INTEGER

random number : 0 is: 25024

Tandom number : 0 is: 25024

In binary it is: 110000111000000

The least significant bit of that number is obviously ==> 0
So therefore bit number 1 from left is: 0

random number : 1 is: 28864

In binary it is: 111000011000000

The least significant bit of that number is obviously ==> 0
So therefore bit number 2 from left is: 0

random number : 2 is: 25294

In binary it is: 110001011001110

The least significant bit of that number is obviously ==> 0
So therefore bit number 3 from left is: 0

random number : 3 is: 1535

In binary it is: 10111111111

The least significant bit of that number is obviously ==> 1
So therefore bit number 4 from left is: 1

random number : 4 is: 4316

In binary it is: 1000011011100

The least significant bit of that number is obviously ==> 0
So therefore bit number 5 from left is: 0

32-bit Padded random integer: 0000000000000000000000000100111

THIS IS A SAMPLE FOR AN UNSUCCESSFUL PRIMALITY CHECK

Checking the integer: 115 , Using a= 58

_	i 	X[i]	z	У	У
	6	1	1	1	 58
	5	1	58	29	72
	4	1	72	9	62
	3	0	62	49	49
	2	0	49	101	101
	1	1	101	81	98
	0	0	98	59	59

The integer: 115 is not a prime!

THIS IS A SAMPLE FOR A SUCCESSFUL PRIMALITY CHECK (PERHAPS PRIME)

Checking the integer: 101 , Using a= 79

i	X[i]	Z	У	У
6	1	1	1	79
5	1	79	80	58
4	0	58	31	31
3	0	31	52	52
2	1	52	78	1
1	0	1	1	1
0	0	1	1	1

The integer: 101 is perhaps a prime!

Our n=8989 Our Phi(8989)=8800

Checking if e=5 can be a public key [Extended Euclidean Algorithm]

q	r1	r2	r	s1	s2	s	t1	t2	t
1760	8800	5	0	1	0	1	0	1	-1760

Unfortunately e=5 Does not have a multiplicative inverse in Z(8800), so we go ahead and try the next e

Checking if e=6 can be a public key [Extended Euclidean Algorithm]

q	r1	r2	r	s1	s2	S	t1	t2	t
1466	8800	6	4	1	0	1	0	1	-1466
1	6	4	2	0	1	-1	1	-1466	1467
2	4	2	0	1	-1	3	-1466	1467	-4400

Unfortunately e=6 Does not have a multiplicative inverse in Z(8800), so we go ahead and try the next e

Checking if e=7 can be a public key [Extended Euclidean Algorithm]

q	r1	r2	r	s1	s2	S	t1	t2	t
1257	8800	7	1	1	0	1	0	 1	-1257
7	7	1	0	0	1	- 7	1	-1257	8800

FOUND IT ! e will be:7 Its multiplicative inverse in Z(8800) is:7543 So, ==> d=7543

```
p = 101
         q = 89
         n = 8989
         e = 7
         d = 7543
As BIT strings:
         p = 1100101
         q = 1011001
         n = 10001100011101
         e = 111
         d = 11101011110111
Here are: r, h(r) and s as bits
r
100000000000000000000000000000111
h(r)=0000000000000000000000000001011011
s =000000000000000000001000000100
Here are: h(r) and s as integers
h(r) = 91
s = 1028
NOT REQUIRED PORTION
=====> Trent's keys: Public => (11, 14351) Private => (1283, 14351)
END OF NOT REQUIRED PORTION
So here is Alice's certificate
Alice cert.name= Alice
Alice cert.e = 7
Alice cert.r
00000000000000000000000000000111
Alice cert.s
         = 1028
```

Alice's 'n' in 32 bits is:0000000000000000001000110011101

K ===> Bob found first '1' from left of 'n' in position ===> K= 13

So the u composed by Bob (according to the specs):

u[b] = 000000000000000000010111110011111

This u as integer is =========== u =6047

So Bob sends to Alice u= 6047

And then Alice [after hashing and decrypting with her private key] returns to Bob v = 603

Showing Bob's encryption of V = E(V, e)_____

i 	X[i]	Squaring Y	Multiplying Y
3	1	1^2(mod 8989)= 1	603x 1(mod 8989)= 603
2	1	603^2(mod 8989)= 4049	$603x \ 4049 \pmod{8989} = 5528$
1	1	5528^2(mod 8989)= 5173	603x 5173(mod 8989)= 136

Bob encrypts v with Alice's public key and gets Z= 136 Bob also does hash of: 6047 which in binary is: 0000000000000000000001011110011111 and he gets h(u) = 136

AND IF THEY MATCH [Z == h(u)], BOB KNOWS HE IS TALKING TO SOMEONE WHO'S GOT ALICE'S PRIVATE KEY (HOPEFULLY ALICE)

TO SUMMARIZE

In Integers:

```
u = 6047
h(u) = 136
V=D(d,h(u)) = 603
E(e,V) = 136
```

In Binary:

```
\begin{array}{lllll} u & = & 0000000000000000001011110011111 \\ h(u) & = & 0000000000000000000000001001000 \\ V = D(d, h(u)) & = & 000000000000000000000010011011 \\ E(e, V) & = & 00000000000000000000000010001000 \end{array}
```